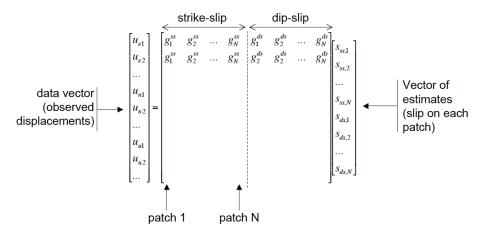
ERTH 455 / GEOP 555 Geodetic Methods

– Lecture 26: Modeling - Slip Inversion cont'd –

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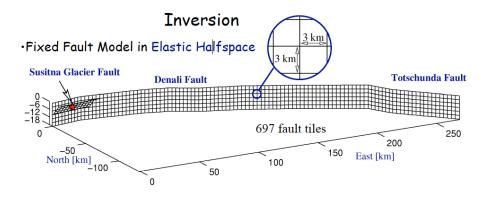
November 20, 2017

Solving for Slip



Eric Calais

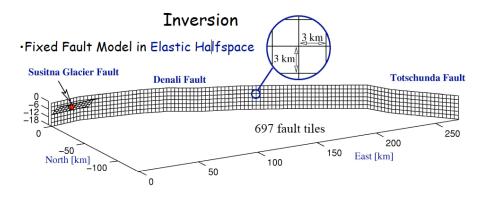
Solving for Slip



Sigrun Hreinsdottir

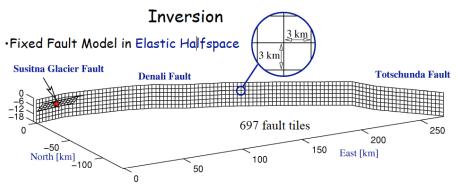
With 224 GPS sites and 697 fault tiles solving for dip-slip and strike-slip, what problem are we running into?

Solving for Slip



Sigrun Hreinsdottir

With 224 GPS sites and 697 fault tiles solving for dip-slip and strike-slip, what problem are we running into? Underdetermined system.



Sigrun Hreinsdottir

- observations at 225 GPS sites: 675 data (if vertical helps)
- 697 fault tiles, ss, ds: 1394 unknowns
- no enough data to constrain number of unknowns
- also often an issue: unphysical oscillatory slip

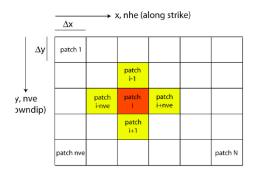
- Idea: Minimize the rate of change of slip with position
- "rate of change of slip" is curvature
- Laplacian:

$$\nabla^2 = \frac{\delta^2}{\delta x^2} + \frac{\delta^2}{\delta y^2} + \frac{\delta^2}{\delta z^2}$$

- Practice: Minimize sum of partial second differentials of slip for each fault patch
- Can be solved using finite-difference method for a function P

$$\frac{\delta^2 P(x)}{\delta x^2} \approx \frac{P(x - \Delta x) - 2P(x) + P(x - \Delta x)}{\Delta x^2}$$

- Our function P(x) is slip s which varies along-strike (x) and down-dip (y)
- For patch *i* finite difference approximation of Laplacian is (nve = number of vertical elements, nhe = horiztonal):



$$I_i = rac{s_{i-nve} - 2s_i + s_{i+nve}}{\Delta x^2} + rac{s_{i-1} - 2s_i + s_{i+1}}{\Delta y^2}$$

Eric Calais

Regularization / Smoothing

• In practice, equation:

$$l_{i} = \frac{s_{i-nve} - 2s_{i} + s_{i+nve}}{\Delta x^{2}} + \frac{s_{i-1} - 2s_{i} + s_{i+1}}{\Delta y^{2}}$$

is written in matrix form, for the along-strike and down-sip components:

The 2 Laplacian matrices are then added:

$$L = L_x + L_y$$

Regularization / Smoothing

• The original problem was:

$$[u] = \begin{bmatrix} G_{ss} & G_{ds} \end{bmatrix} \begin{bmatrix} s_{ss} \\ s_{ds} \end{bmatrix}$$

• now it becomes:

$$\begin{bmatrix} u\\0\\0\end{bmatrix} = \begin{bmatrix} G_{ss} & G_{ds}\\L & 0\\0 & L\end{bmatrix} \begin{bmatrix} s_{ss}\\s_{ds}\end{bmatrix}$$

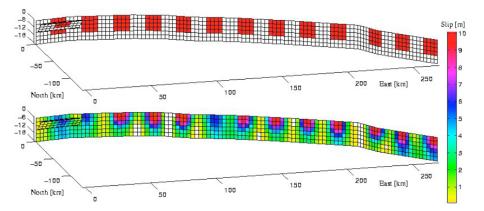
• amount of smoothing can be tuned using scalar smoothing factor κ :

$$\begin{bmatrix} u \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} G_{ss} & G_{ds} \\ \kappa L & 0 \\ 0 & \kappa L \end{bmatrix} \begin{bmatrix} s_{ss} \\ s_{ds} \end{bmatrix}$$

• $\kappa = 0$: no smoothing, $\kappa = 1$ maximum smoothing

Regularization / Smoothing

What can you recover? Checker board / Resolution test:



Sigrun Hreinsdottir

Distributed Slip Inversion

This is how you get this:

